

REVIEW OF CONSUMER THEORY

CHAPTER 1

UTILITY FUNCTIONS

- ❑ Describe how much “happiness” or “satisfaction” an individual experiences from “consuming” goods – the **benefit** of consumption

- ❑ **Marginal Utility**
 - ❑ The extra total utility resulting from consumption of a small/incremental extra unit of a good
 - ❑ Mathematically, the (partial) slope of utility with respect to that good

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 - ❑ Diminishing marginal utility

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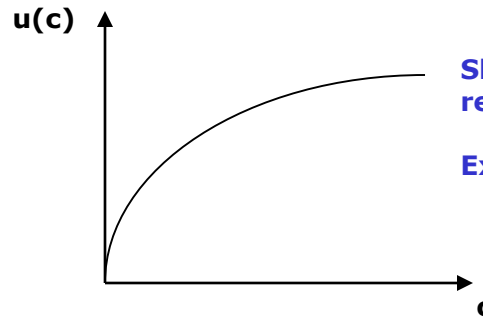
- ❑ **Two-good case:** $u(c_1, c_2)$, with $u_i(c_1, c_2) > 0$ and $u_{ii}(c_1, c_2) < 0$ for each of $i = 1, 2$
 - ❑ Utility strictly increasing in **each good** individually (partial)
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 - ❑ Diminishing marginal utility in **each good** individually
- ❑ Easily extends to N -good case: $u(c_1, c_2, c_3, c_4, \dots, c_N)$

UTILITY FUNCTIONS

□ **One-good case**

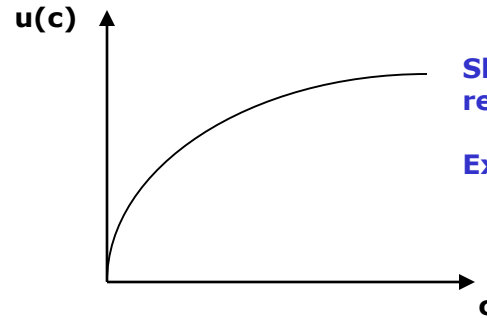


Slope (marginal utility) asymptotes to (but never reaches...) zero

Example: $u(c) = \ln c$ or $u(c) = \text{sqrt}(c)$

UTILITY FUNCTIONS

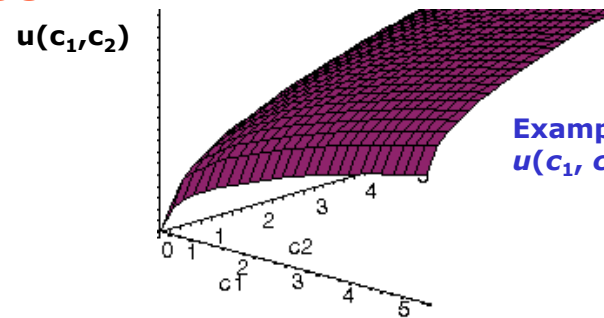
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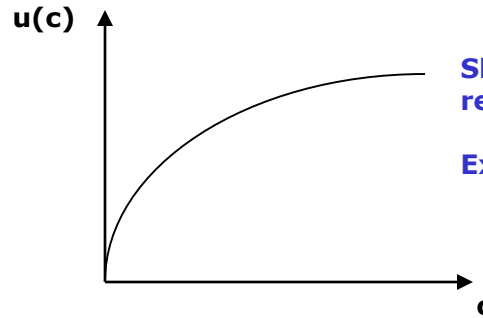
Two-good case



Example: $u(c_1, c_2) = \ln c_1 + \ln c_2$ or
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UTILITY FUNCTIONS

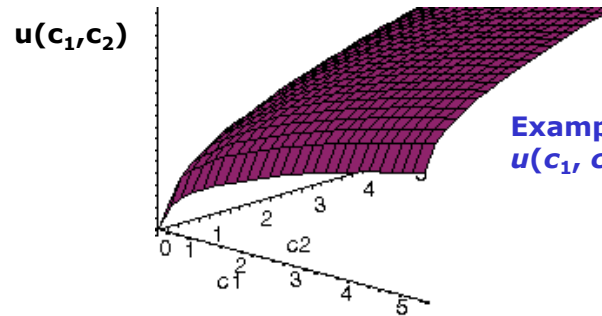
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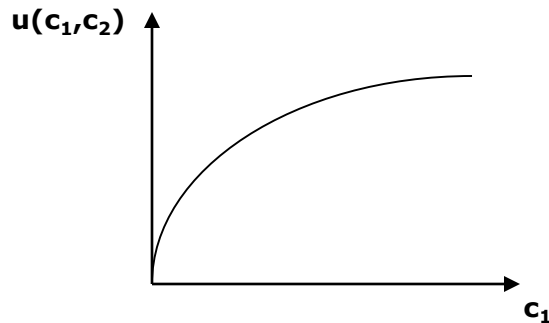
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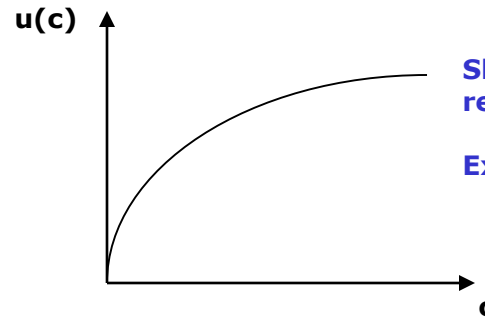
Example: $u(c_1, c_2) = \ln c_1 + \ln c_2$ or $u(c_1, c_2) = \sqrt{c_1} + \sqrt{c_2}$

Viewed in good-by-good space



UTILITY FUNCTIONS

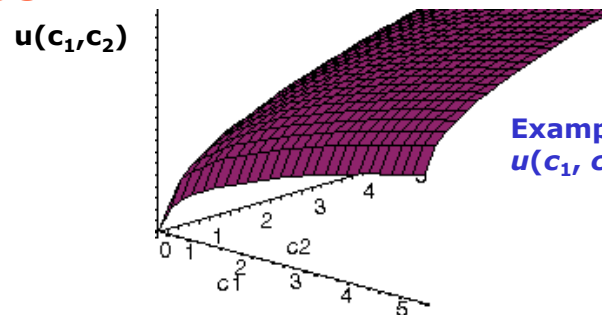
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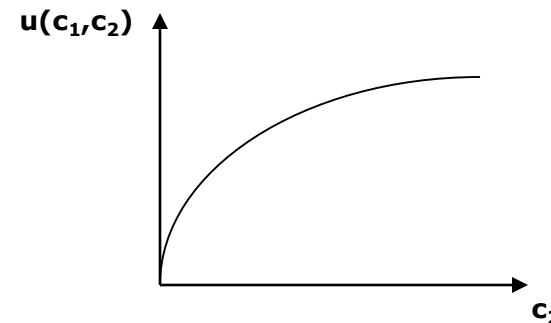
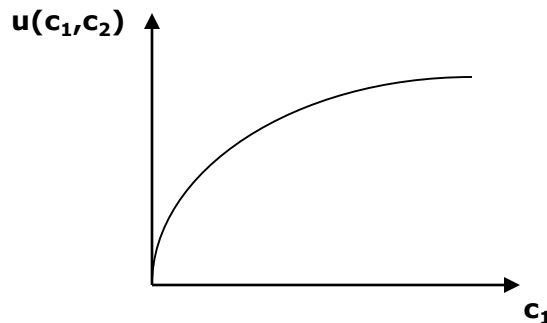
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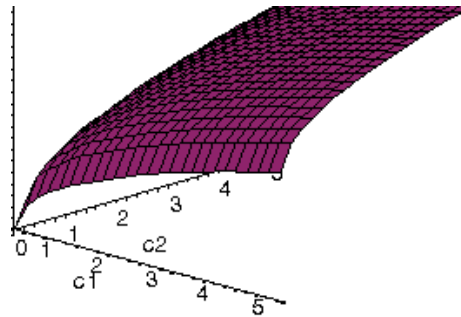
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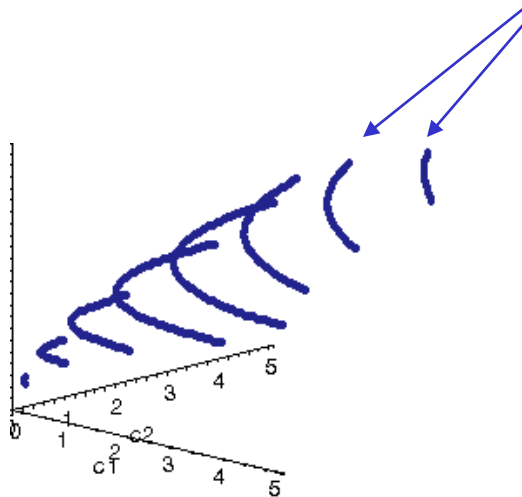


UTILITY FUNCTIONS

Alternative views



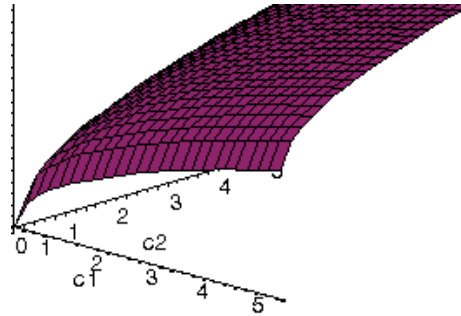
Emphasizing the contours



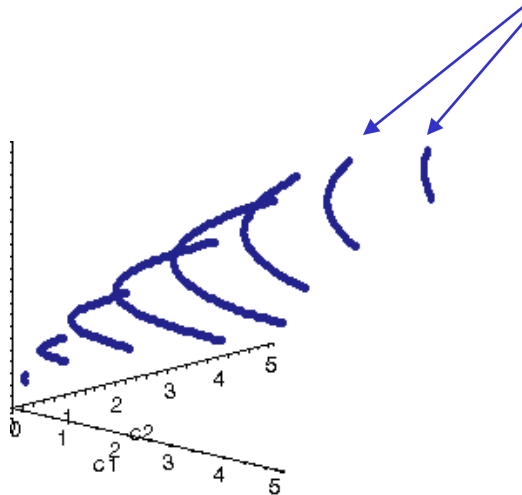
Indifference Curve: the set of all consumption bundles that deliver a particular level of utility/happiness

UTILITY FUNCTIONS

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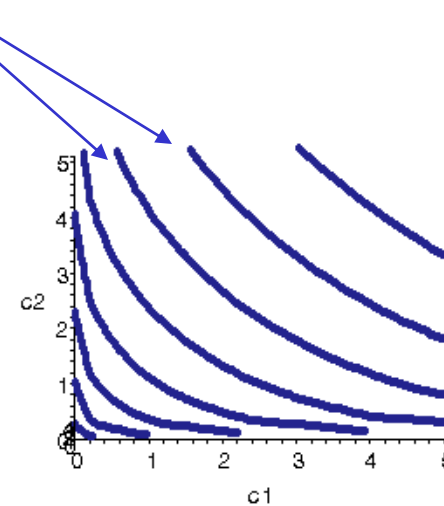


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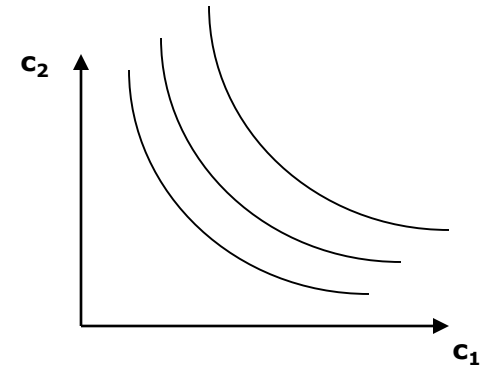
Indifference Curve: the set of all consumption bundles that deliver a particular level of utility/happiness

Viewing only the contours



UTILITY FUNCTIONS

- **Marginal Rate of Substitution (MRS)**
 - **Maximum** quantity of one good consumer is **willing** to give up to obtain **one** extra unit of the other good
 - Graphically, the (negative of the) slope of an indifference curve
 - MRS is itself a **function** of c_1 and c_2 (i.e., $MRS(c_1, c_2)$)



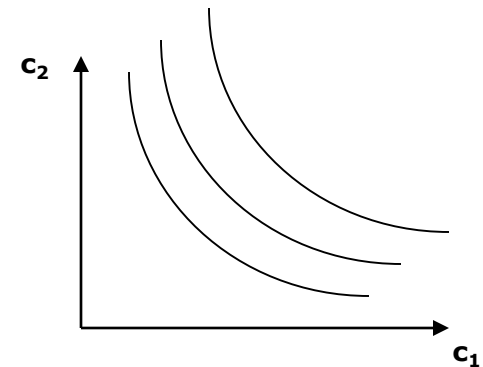
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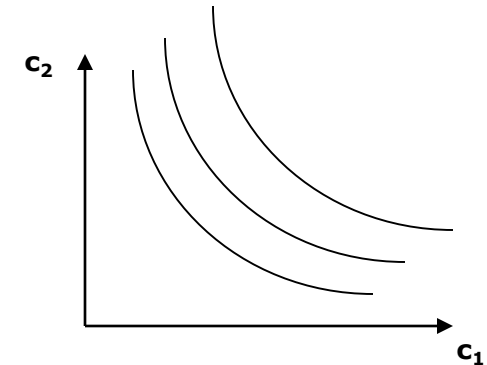
- **MRS equals ratio of marginal utilities**

- $$MRS(c_1, c_2) = \frac{u_1(c_1, c_2)}{u_2(c_1, c_2)}$$

- Using Implicit Function Theorem (see Practice Problem Set 1)

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$$MRS(c_1, c_2) = \frac{u_1(c_1, c_2)}{u_2(c_1, c_2)}$$
 - ❑ Using Implicit Function Theorem
- ❑ **Summary: whether graphically- or mathematically-formulated, utility functions describe the benefit side of consumer optimization**



BUDGET CONSTRAINTS

- ❑ Describe the **cost** side of consumption

- ❑ **One-good case (trivial):** $Pc = Y$
 - ❑ Assume income Y is taken as given by consumer for now...

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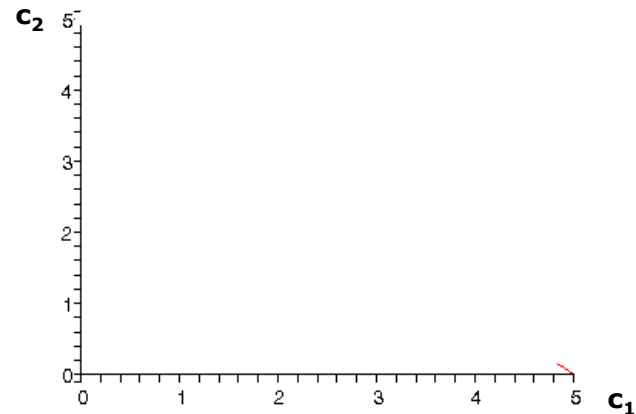
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Plotted in 2D-consumption-space



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$$P_1c_1 + P_2c_2 = Y$$



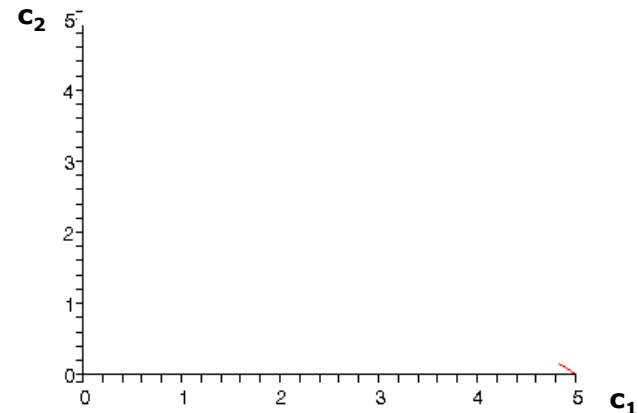
$$P_2c_2 = -P_1c_1 + Y$$



$$c_2 = -\frac{P_1}{P_2}c_1 + \frac{Y}{P_2}$$

Isolate c_2 to
graph the budget
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Plotted in 2D-consumption-space



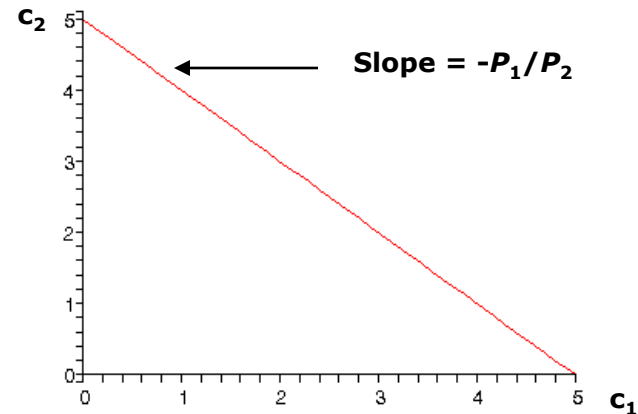
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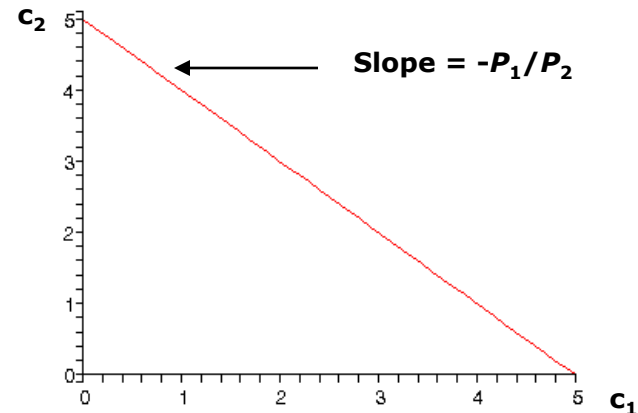


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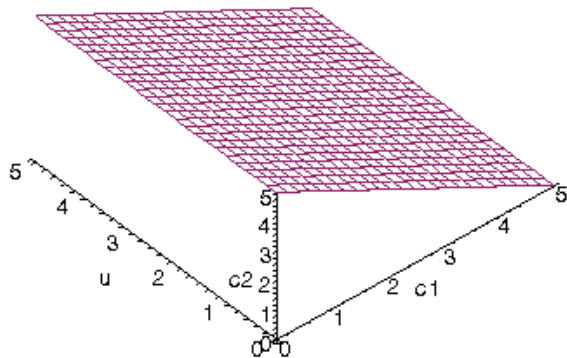
Plotted in 2D-consumption-space



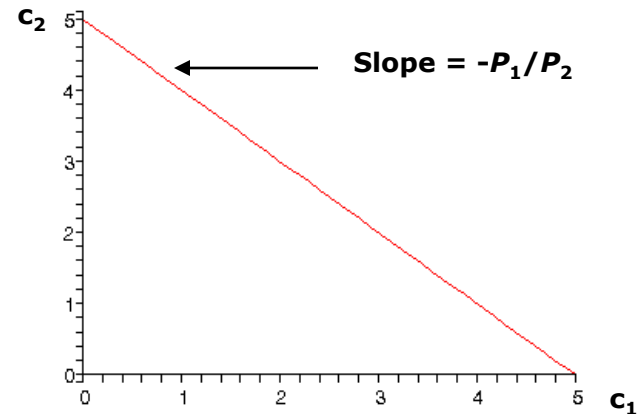
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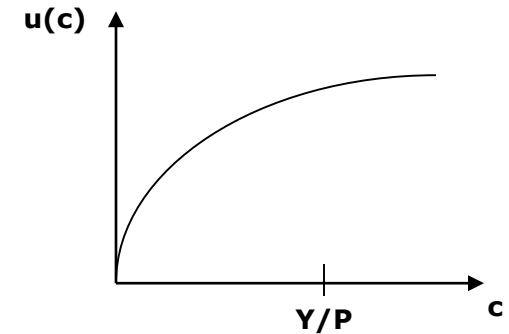


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- **Consumer's decision problem:** maximize utility subject to budget constraint – bring together both **cost** side and **benefit** side

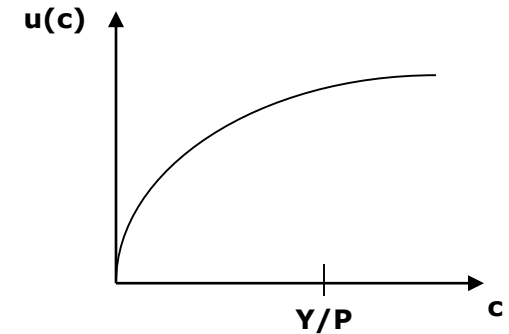
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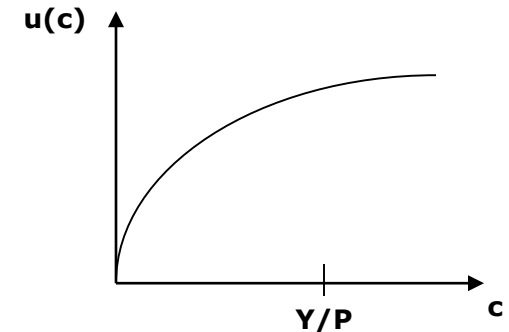
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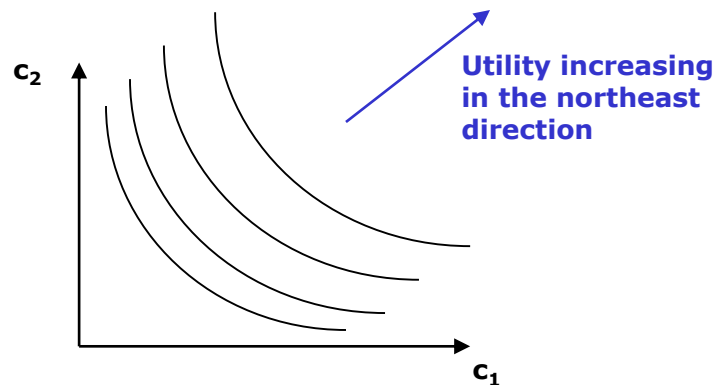
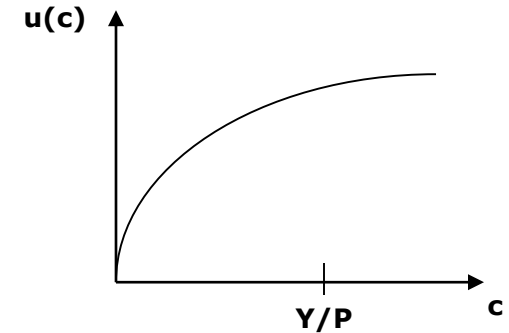
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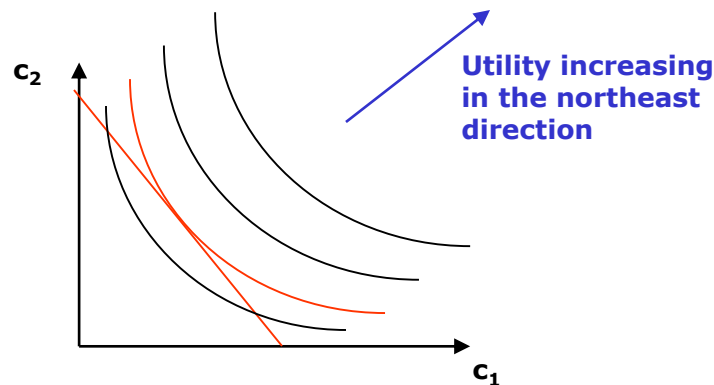
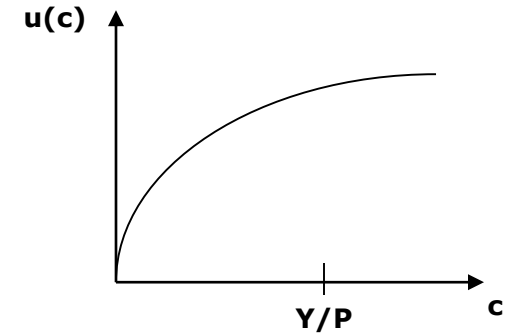
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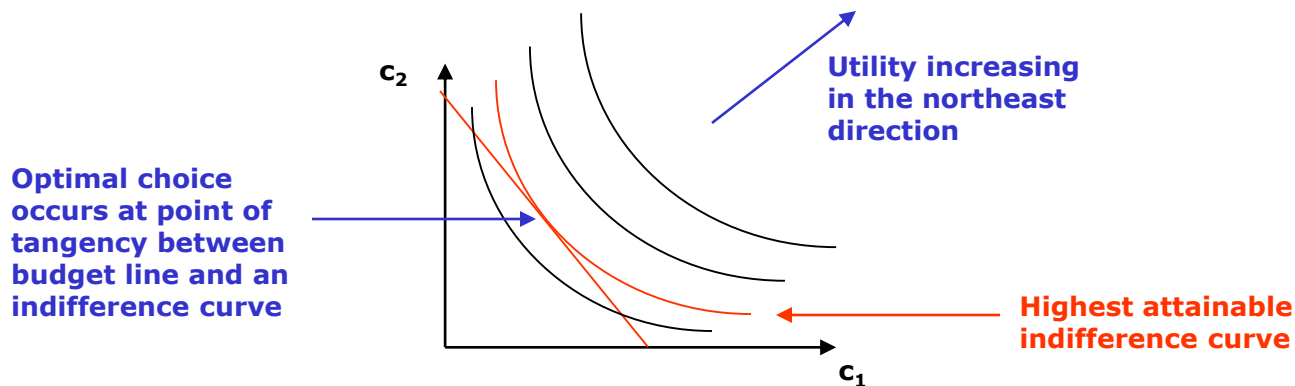
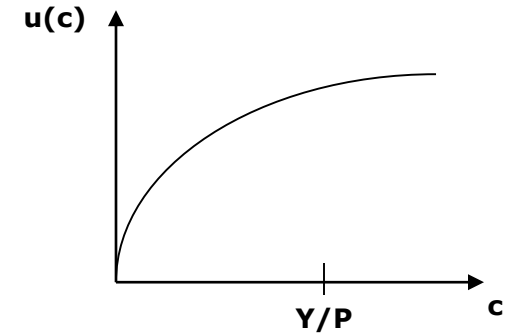
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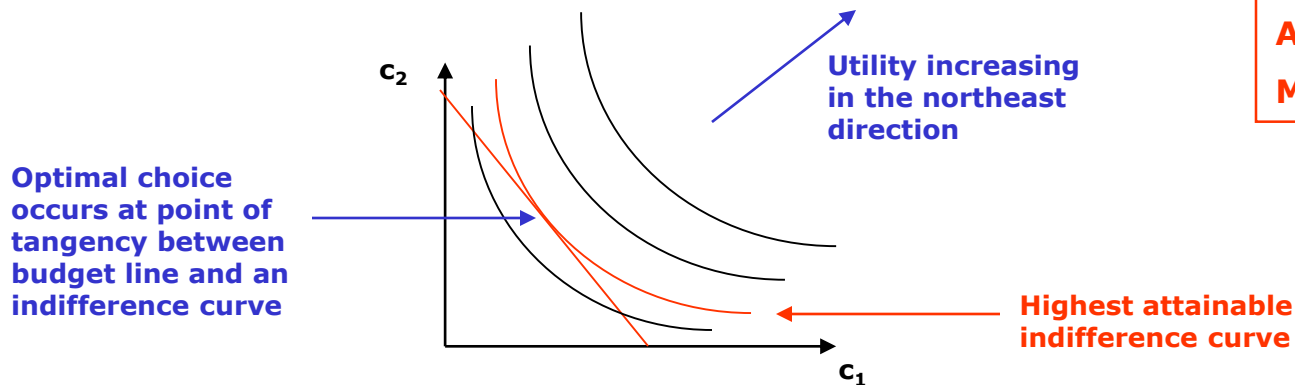
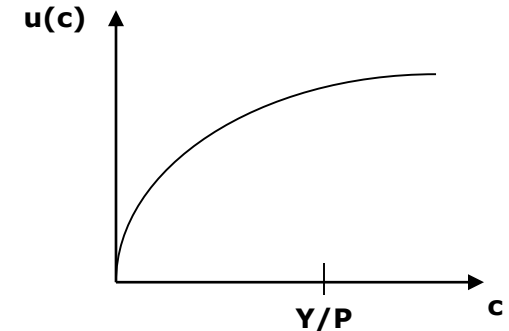
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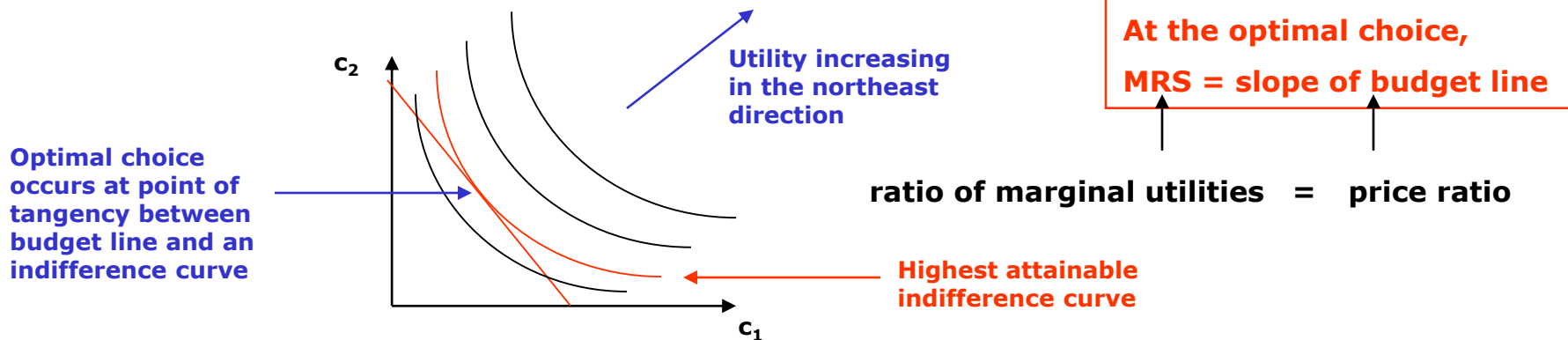
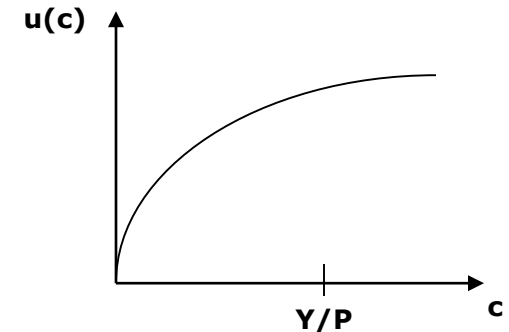
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OPTIMALITY CONDITION:
 At the optimal choice,
MRS = slope of budget line

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 - **Maximize some function (economic application: utility function)...**
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 - ❑ **...subject to the constraint $g(x,y) = 0$ (**Note formulation of constraint**)**

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Lagrange multiplier

$$L(x, y, \lambda) = f(x, y) + \lambda g(x, y)$$

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 - ❑ **Step 2: Compute first-order conditions with respect to $x, y,$ and λ**
 - 1) $f_x(x, y) + \lambda g_x(x, y) = 0$

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- ❑ **Lagrange Method: mathematical tool to solve constrained optimization problems**

- ❑ **General mathematical formulation**
 - ❑ **Choose (x, y) to maximize a given objective function $f(x,y)$...**
 - ❑ **...subject to the constraint $g(x,y) = 0$ (Note formulation of constraint)**
 - ❑ **Step 1: Construct Lagrange function** Lagrange multiplier

$$L(x, y, \lambda) = f(x, y) + \lambda g(x, y)$$
 - ❑ **Step 2: Compute first-order conditions with respect to x , y , and λ**
 - 1) $f_x(x, y) + \lambda g_x(x, y) = 0$
 - 2) $f_y(x, y) + \lambda g_y(x, y) = 0$

LAGRANGE ANALYSIS

- ❑ **Consumer optimization a **constrained optimization** problem**
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Lagrange multiplier

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2) $f_y(x, y) + \lambda g_y(x, y) = 0$

3) $g(x, y) = 0$

Rationale: setting first derivatives to zero isolates maxima (or minima...technically, need to check second-order condition...)

LAGRANGE ANALYSIS

- **Step 3:** Solve the system of first-order conditions for x , y , and λ
 - Often most interested in simply eliminating the multiplier...

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□ **Optimality condition: at the optimum (x^* , y^*)**

$$\frac{f_x(x^*, y^*)}{f_y(x^*, y^*)} = \frac{g_x(x^*, y^*)}{g_y(x^*, y^*)}$$

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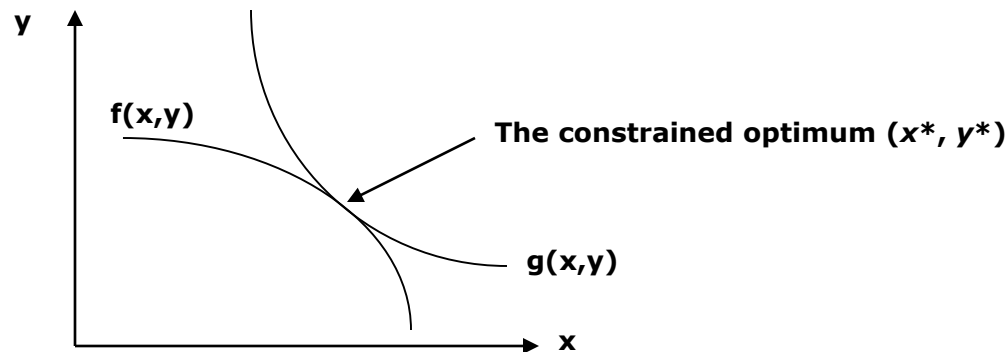
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$$\frac{f_x(x^*, y^*)}{f_y(x^*, y^*)} = \frac{g_x(x^*, y^*)}{g_y(x^*, y^*)}$$

Graphical interpretation: at the constrained optimum, the function $f(\cdot)$ is tangent to the function $g(\cdot)$



LAGRANGE ANALYSIS

- ❑ **Apply Lagrange tools to consumer optimization**
- ❑ **Objective function: $u(c_1, c_2)$**
- ❑ **Constraint: $g(c_1, c_2) = Y - P_1c_1 - P_2c_2 = 0$**

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$$1) \quad u_1(c_1, c_2) - \lambda P_1 = 0$$

$$2) \quad u_2(c_1, c_2) - \lambda P_2 = 0$$

$$3) \quad Y - P_1c_1 - P_2c_2 = 0$$

- ❑ **Step 3: Solve (focus on eliminating multiplier from eqns 1 & 2)**

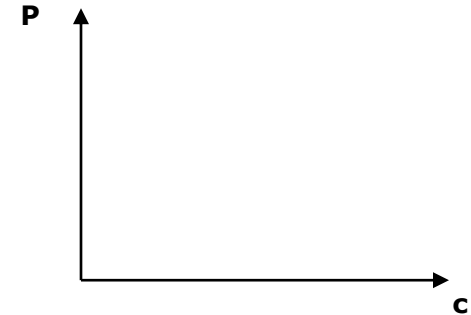
$$\frac{u_1(c_1^*, c_2^*)}{u_2(c_1^*, c_2^*)} = \frac{P_1}{P_2}$$

OPTIMALITY CONDITION

i.e., MRS = price ratio

THE THREE MACRO (AGGREGATE) MARKETS

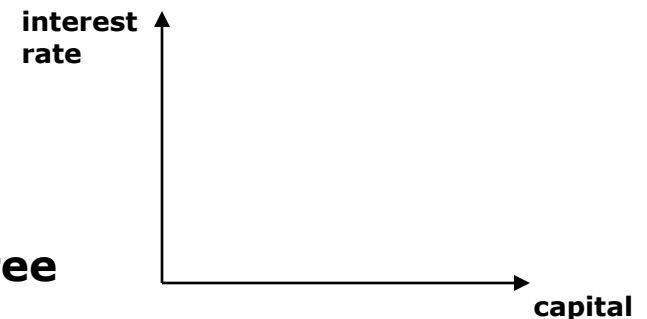
❑ **Goods Markets**



❑ **Labor Markets**



❑ **Financial/Capital/Savings/Asset Markets**



❑ **Will put micro-foundations under all three**