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Full Length Articles Interest rate uncertainty and sovereign default risk

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ABSTRACT

Empirical studies suggest that fluctuations in the level and volatility of the world interest rate affect sovereign spreads in emerging economies. We incorporate an estimated time-varying process for the world interest rate (with both level and volatility shocks) into a model of sovereign default calibrated to a panel of emerging economies. Time variation in the world interest rate interacts with default incentives in the model and leads to state contingent effects similar to the empirical literature. On average, in response to a rise in the world interest rate the model delivers a 1.4 times increase in the spread. The volatility state has a major impact on this average – the increase in spreads is much larger in high volatility states. Moreover, we show that fluctuations in the world interest rate can generate considerable co-movement in sovereign yields across nations, as seen in the data.

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1. Introduction

The emerging economy business cycle literature has shown that shocks to country spreads play an important role in accounting for domestic business cycles. In addition, a large body of empirical work has traced variation in emerging economy spreads and default risk to both domestic and global factors.¹ Motivated by this work, the sovereign default literature provides a framework in which time varying default probabilities generate endogenous variation in sovereign yields.² However, this literature has emphasized the role of domestic factors with little attention to the global interlinkages highlighted by the empirical work.³ Our paper addresses this gap by focusing on the relationship between uncertainty in the world interest rate and sovereign default risk, while also retaining a role for domestic factors. Our focus on variation in the world interest rate as a global factor is consistent with several studies. For example, González-Rozada and Yeyati (2008) finds that movements in US treasuries as well as in proxies for global risk explain about half of the long run volatility in emerging economy interest rates.⁴

Some recent episodes highlight the importance of the behavior of US interest rates for world debt markets. A notorious example, usually referred to as the "taper tantrum," occurred in May of 2013 when former US Fed chairman Ben Bernanke suggested the possibility of a reduction in future bond purchases by the Fed. This triggered a sharp market adjustment in emerging market economies featuring a reversal in capital flows and a spike in government bond yields. On average, sovereign yields across emerging economies rose by 1% (Rai and Suchanek, 2014). An example of policy makers' dislike of uncertainty about the world interest rate occurred in 2015, as summarized by the following quotes reported in the Financial Times (September 9, 2015):

"We think US monetary policymakers have got confused about what to do. The uncertainty has created the turmoil."

Mirza Adityaswara, Sr. Deputy Governor, Central Bank of Indonesia.

"The uncertainty about when the Fed hike will happen is causing more damage than the Fed hike will itself."

Julio Velarde, Governor, Central Bank of Peru.

Motivated both by the empirical evidence on the importance of global factors in the movement of emerging economies' sovereign spreads as well as recent events and policy makers' concerns, we develop an equilibrium model of sovereign default (in the tradition of Eaton and Gersovitz, 1981) to study the relationship between endogenous country spreads and movements in both the level and the volatility of the world interest rate. To do so, we introduce stochastic volatility into the process of the world interest rate (following Fernández-Villaverde et al., 2011) in an otherwise standard quantitative model of long term sovereign debt (as in Hatchondo and Martinez, 2009). We use the model to quantify the role that shocks to the world interest rate play in explaining variation in sovereign spreads and the borrowing levels chosen by the sovereign, as well as the cross-country correlation in borrowing costs induced by the world interest rate process.

Our model implies that the impact of shocks to the world interest rate are highly state contingent and depend on income and existing debt levels, as well as on the state of world interest itself (its level and volatility). We find that on average the spread response is 1.4 times the increase in the world interest rate when volatility and the debt level are held constant at their means. This 'slope' increases to 6.4 when volatility state is high (4 standard deviations above mean) and falls to 0.8 when volatility is low (4 standard deviations below mean). Not surprisingly, a higher debt level makes the spread response to the world interest rate stronger and below-average debt lowers the response. Interestingly, these 'spread slopes' are in line with the empirical evidence (a spread slope of roughly 1), presented in Foley-Fisher and Guimaraes (2013) and Arora and Cerisola (2001). We also find that debt issuance declines when the world interest rate rises and this responsiveness is higher in the high volatility state.

Since our model can be viewed as a mechanism that transmits shocks in the process for the world interest rate into fluctuations in default probabilities and hence in sovereign spreads, we can use the model to infer how much cross-country comovement in spreads is generated by this "global factor." We find that when two economies (with income processes as correlated as in the data) face a constant world interest rate, their sovereign yields display a low correlation (0.17 and insignificant). However, if they face a common time-varying process for the world interest rate the co-movement between their sovereign yields increases significantly: the correlation is now 0.40 and significant. This is close to the mean correlation observed in the data (0.53).

The rest of the paper is organized as follows. Section 2 briefly reviews the related literature. Section 3 describes the model and defines the equilibrium. Section 4 discusses the numerical solution and the calibration. Section 5 presents the results and Section 6 concludes. An appendix presents details about our data as well as additional results and robustness exercises.

¹ See early work in Edwards, 1984, Cantor and Packer, 1996 and Eichengreen and Mody, 2000. For some recent examples of studies that highlight global factors, see Hilscher and Nosbusch (2010), González-Rozada and Yeyati (2008) Akıncı (2013), and Maltritz (2012).

² We use the terms "sovereign" and "government" interchangeably throughout the paper.

³ Below we discuss a few papers that do highlight the role of global risk aversion.

⁴ These findings are re-iterated using a variety of empirical methods and proxies for global risk, different time periods, and different countries in other work. For example, Akıncı (2013) uses a structural VAR on a panel of emerging economies while Maltritz (2012) uses Bayesian model averaging on a panel of European nations and both replace the high yield spreads used by González-Rozada and Yeyati (2008) (as a measure of global risk) with corporate bond spreads captured by BAA bonds. Hilscher and Nosbusch (2010) add VIX as a measure of global uncertainty and find that it is statistically significant in explaining credit default swap (CDS) spreads of Mexico, Turkey, and Korea.

2. Related literature

There is ample evidence that movements in the international risk-free rate (usually proxied by the US T-bill rate) have macroeconomic consequences for emerging economies. Neumever and Perri (2005) report that real country interest rates in emerging economies are strongly countercyclical and tend to lead the cycle. They also find that exogenous interest rate shocks can account for up to 50% of the volatility of output in Argentina. Uribe and Yue (2006) find a strong relationship between the world interest rate, the country spread and emerging market fundamentals. In particular, they show that US interest rate shocks and country spread shocks can explain the large movements seen in the aggregate activity of emerging economies. García-Cicco et al. (2010) also find that the country spread shock is one of the most important drivers of emerging economies business cycles. All these papers take the country spread as an exogenous variable with a time-invariant volatility, while our work endogenizes both the level and the time-varying volatility of the spread (as a result of default incentives on the part of the sovereign).⁵ There are also a number of empirical papers that include U.S. monetary policy variables (including interest rates) as determinants of sovereign spreads. Arora and Cerisola (2001) explore the empirical determinants of sovereign spreads using data from 11 emerging economies with special emphasis on US monetary policy and using controls typical in the literature. Like us, they find that the level of spreads is increasing in the level of the interest rate as well as a proxy of volatility.⁶ Foley-Fisher and Guimaraes (2013), using a different methodology (identification through heteroskedasticity), also find that an unexpected increase in US inflation-indexed bond vields increases sovereign spreads: a one-percent increase in world interest rates raises sovereign spreads by roughly 0.8 to 1%⁷ As mentioned above, our model-based findings are in line with the empirical evidence from these two studies.

Fernández-Villaverde et al. (2011) study the impact of exogenous time-varying volatility on the macroeconomic dynamics of a small open economy. They examine the effects on the business cycles of Argentina, Ecuador, Venezuela, and Brazil. We follow their approach to modeling the stochastic behavior of the world interest rate, while departing from their approach to modeling the country spread: as already noted, our model is one of endogenous spreads. Then, we explore the mechanism by which world interest rate uncertainty affects the country spreads and default risk in emerging economies. We see our work as complementary to theirs. Guimaraes (2011) highlights the importance of shocks to the level of world interest rates in a theoretical sovereign default model. His work differs from ours in that it does not consider time variation in the volatility of the world interest rate and does not carry out a quantitative evaluation of the model.

Our paper builds on the quantitative literature on sovereign defaults (following Eaton and Gersovitz, 1981, Aguiar and Gopinath, 2006, and Arellano, 2008). Lizarazo (2013) explores how risk aversion on the part of international lenders influences debt and default dynamics of the borrowing country and therefore how the risk premium affects sovereign spreads. Verdelhan and Borri (2010) also explore the role of time-varying risk aversion of lenders in a model with many small open economies that have endowments which are partially correlated with the lender's endowment process. They also find that risk aversion plays an important role in determining spreads and borrowing levels. Building on these two papers, we incorporate risk aversion in our modeling of foreign lenders.

Within the sovereign debt literature, our paper is particularly related to two recent studies. Seoane (2019) studies how changes in aggregate income volatility affect sovereign spreads of Greece, Italy, Portugal, and Spain. He extends the model in Arellano (2008) to include time-varying volatility of the income process which generates substantial variability in spreads. Our work complements his: we keep the income process with a time-invariant volatility and introduce time-varying volatility in the world interest rate process. The second paper is the one by Pouzo and Presno (2016). They study the problem of a small open economy that can default on its obligations in the presence of model uncertainty. In their work, lenders fear that the probability model of the underlying state of the borrowing economy is misspecified and hence may demand higher returns on their investments. Even though we tackle a different type of uncertainty (i.e. time-varying volatility of the world interest rate) the results are consistent: more uncertainty leads to higher and more volatile spreads.⁸

Finally, our paper is also related to the literature on uncertainty shocks in macroeconomic models.⁹ For instance, Justiniano and Primiceri (2008) and Bloom (2009) study the effect of changes in the volatility of technology shocks in general equilibrium models for closed economies. Justiniano and Primiceri (2008) study the changes in volatility in postwar US data by estimating a large-scale dynamic stochastic general equilibrium model allowing for time variation in the structural innovations. They find that shocks specific to investment are mostly responsible for the observed "great moderation." Bloom (2009), on the other hand, shows that uncertainty shocks can generate short sharp recessions and recoveries.

⁵ In a recent study, Reyes-Heroles and Tenorio (2017) document the existence of two regimes in the volatility of interest rates at which emerging economies borrow and show that these regimes are closely related to the occurrence of sudden stops in these economies.

⁶ Unlike us, Arora and Cerisola (2001) use the federal funds rate as their measure of interest rate and their volatility proxy is constructed from the estimated values of the conditional standard error from an ARCH model for the difference between the three-month U.S. treasury bill yield and the federal funds rate. Despite these differences our findings are similar to their empirical results.

⁷ Longstaff et al. (2011) and Fender et al. (2012) also include a measure of US interest rates in their study of the determinants of sovereign CDS data.

⁸ Another study in the sovereign debt literature that deals with time-varying volatility is Gu and Stangebye (2017). They study costly information acquisition in a model of defaultable debt and show how this can create time-varying volatility in the spread.

⁹ Fernández-Villaverde and Rubio-Ramírez (2013) and Bloom (2014) provide thorough accounts of the growing literature dealing with uncertainty shocks and timevarying volatility in macroeconomics.

3. Model

We consider a small open economy populated by a continuum of households. The economy trades long-duration non-statecontingent bonds with a mass of competitive foreign lenders and has no commitment to repaying its debts. The world interest rate (which matters for bond prices) is time-varying. Time is discrete and goes on forever: t = 0,1,2,...

3.1. Domestic economy

There is a single tradable good. As is standard in the sovereign default literature, the economy receives a stochastic endowment stream of this good y_{tr} where

$$\log(y_t) = \rho_y \log(y_{t-1}) + \varepsilon_t^y \tag{1}$$

with $|\rho_y| < 1$, and $e_x^t \sim N(0, \sigma_{\varepsilon}^2)$. The government's objective is to maximize the expected life-time utility of the representative agent in the economy, namely

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t u(c_t) \tag{2}$$

where \mathbb{E} denotes the expectation operator, c_t is consumption, $\beta \in (0,1)$ denotes the subjective discount factor, and the $u(\cdot)$ is a period utility function which satisfies u' > 0, u'' < 0.

Each period, the government makes two decisions. First, it decides whether to default. Second, it chooses the number of bonds that it purchases or issues in the current period.

The government has access to an international financial market where it trades long-duration non-contingent bonds with competitive foreign investors at a price q_t . As in Hatchondo and Martinez (2009), we assume that a bond issued in period t promises an infinite stream of coupons, which decrease at a constant rate δ . In particular, a bond issued in period t promises to pay one unit of the good in period t + 1 and $(1 - \delta)^{s-1}$ units in period t + s, with $s \ge 2$. Let $b_t (b_{t+1})$ denote the number of outstanding coupon claims at the beginning of the current (next) period. A positive value of b_t implies that the government was a net issuer of bonds in the past. The number of bonds issued by the government is given by $[b_{t+1} - (1 - \delta)b_t]$. The resource constraint for the repayment case is then given by:

$$c_t + b_t = y_t + q_t [b_{t+1} - (1 - \delta)b_t]$$
(3)

If the government declares a default, it is excluded from financial markets and remains in financial autarky for a stochastic number of periods. While the government is in default, it cannot issue debt and domestic aggregate income is reduced by $\phi(y)$. As in Arellano (2008) and Chatterjee and Eyigungor (2012), we assume that it is proportionally more costly to default in good times ($\phi(y)/y$ is increasing in y).¹⁰ Following most studies of sovereign default, the income-cost of defaulting is not a function of the size of the default.¹¹ Thus, when the government defaults, it does so on all current and future debt obligations. As argued in Hatchondo et al. (2016), this is consistent with the behavior of defaulting countries.¹² Following previous studies, we also assume that the recovery rate for debt in default is zero. The resource constraint for the default case is given by:

$$c_t = y_t - \phi(y_t). \tag{4}$$

3.2. Foreign lenders

Foreign creditors are risk averse and their stochastic discount factor is given by:

$$m_{t,t+1} = e^{-r_{t+1} - \kappa_y \left(\varepsilon_{t+1}^y + 0.5\kappa_y \sigma_{\varepsilon}^2\right)}, \quad \text{with} \quad \kappa_y \ge 0.$$
(5)

This formulation introduces a positive risk premium because bond payoffs are more valuable to lenders in states in which the government is more likely to default (i.e., in states in which income shocks in the domestic economy, ε^{ν} , are low). Here, *r* is the

¹⁰ Arellano (2008) and Chatterjee and Eyigungor (2012) show that this property is important in accounting for the dynamics of the sovereign debt interest rate spread. Mendoza and Yue (2012) show that this property of the cost of defaulting arises endogenously in a setup in which defaults affect the ability of local firms to acquire a foreign intermediate input good.

¹¹ See Sosa-Padilla (2018) for a model of endogenous default costs, where the output cost of default is a function of the amount of debt that is defaulted upon.

¹² Sovereign debt contracts often contain acceleration and cross-default clauses. These clauses imply that after a default event, future debt obligations become current. The type of acceleration clauses depend on the details of each bond contract and on the jurisdiction under which the bond was issued (see IMF, 2002). For instance, in some cases it is necessary that creditors holding a minimum percentage of the value of the bond issue request their debt to be accelerated for their future claims to become due and payable. In other cases, no such qualified majority is needed.

time-varying world interest rate, and κ_y is the parameter governing the magnitude of the risk premium. A higher value of κ_y can be seen as capturing how correlated the small open economy is with respect to the lenders' income process, or alternatively, the degree of diversification in foreign lenders' portfolios.¹³

Bonds are priced in a competitive market inhabited by a large number of identical lenders, which implies that bond prices are pinned down by a zero expected profit condition. The price per bond is then given by:

$$q_t = \mathbb{E}_t \Big\{ m_{t,t+1} \big(1 - d_{t+1} \big) \big[1 + (1 - \delta) q_{t+1} \big] \Big\}$$
(6)

where d_{t+1} and q_{t+1} represent the government's default decision and equilibrium bond price in period t + 1, respectively.

3.3. Law of motion for the world interest rate

Following Fernández-Villaverde et al. (2011) we specify the international risk-free rate faced by investors as:

$$r_t = \overline{r} + \varepsilon_{r,t} \tag{7}$$

where \overline{r} is the mean of world risk-free real rate, and $\varepsilon_{r,t}$ represents deviations from this mean. In particular, we assume the following AR(1) behavior for $\varepsilon_{r,t}$:

$$\varepsilon_{r,t} = \rho_r \varepsilon_{r,t-1} + e^{\sigma_{r,t}} u_{r,t} \tag{8}$$

where $u_{r,t}$ is a normally distributed shock with mean zero and unit variance. The crucial ingredient in this stochastic process is that the standard deviation ($\sigma_{r,t}$) is not constant but time-varying, and itself follows another (independent) AR(1) process:

$$\sigma_{r,t} = \left(1 - \rho_{\sigma_r}\right)\bar{\sigma_r} + \rho_{\sigma_r}\sigma_{r,t-1} + \eta_r u_{\sigma_r,t} \tag{9}$$

where $u_{\sigma_r t}$ is a normally distributed shock with mean zero and unit variance. We further assume that $u_{r,t}$ and $u_{\sigma_r,t}$ are independent of each other. The parameters $\bar{\sigma}_r$ and η_r measure the degree of mean volatility and stochastic volatility in the international risk free rate. A high $\bar{\sigma}_r$ corresponds to a high mean volatility and a high η_r corresponds to a high degree of stochastic volatility in the international risk free rate.

3.4. Timing

The timing of events, for a government that is not excluded from financial markets, is as follows. The government starts with an initial bond position b_t and observes the realizations of the income level (y_t) , the world interest rate level (r_t) and the interest rate volatility $(\sigma_{r,t})$, and then decides whether to repay its outstanding debt. If it decides to repay, it chooses b_{t+1} subject to the resource constraint, taking the bond price schedule $q_t(b_{t+1}; y_t, r_t, \sigma_{r,t})$ as given. Finally, consumption takes place.

On the other hand, if the government decides to default it gets excluded from financial markets and suffers a direct income loss. In case of default, there is no other decision to be made as the level of consumption equals the (reduced) income level. The government will re-access financial markets in the following period with probability μ (and it will remain excluded from financial markets with probability $1 - \mu$).

3.5. Recursive equilibrium

We now turn to recursive notation, where *primes* denote next-period value of the variables. Let $\mathbf{s} = \{y, r, \sigma_r\}$ denote the aggregate exogenous state. Given a number of outstanding coupon claims at the beginning of the next period *b*' and a realization of **s**, the price of a bond satisfies:

$$q(b', \mathbf{s}) = \mathbb{E}_{\mathbf{s}' | \mathbf{s}} \{ m(\mathbf{s}', \mathbf{s}) (1 - d') [1 + (1 - \delta) q(b'', \mathbf{s}')] \}$$
(10)

where *d'* is the next-period default decision, and *b''* is the next-period debt choice. The optimal default decision is taken as:

$$\nu^{0}(b;\mathbf{s}) = \max_{d \in \{0,1\}} \left\{ (1-d)\nu^{c}(b;\mathbf{s}) + d\nu^{d}(\mathbf{s}) \right\}$$
(11)

¹³ This modeling of risk-averse foreign lenders follows Vasicek (1977) and has been used recently in the sovereign debt literature (Arellano and Ramanarayanan, 2012, Bianchi and Sosa-Padilla, 2020, etc.). The functional form for the lenders' stochastic discount factor (SDF) makes it explicit that the variance of the domestic income matters, but it is less clear that the variance of r_t also affects the SDF through the level of r_t (see Eq. (8)). Since r_t is time-varying its volatility will induce additional time variation in the SDF. The appendix shows that our results are robust to using a richer specification for (5) (one that explicitly includes the variance of r_t).

where d equals 1 (0) if the government chooses to (not to) default. Under no-default, the government solves the following problem:

$$v^{c}(b;\mathbf{s}) = \max_{b'} \left\{ u(y + q(b';\mathbf{s})(b' - (1 - \delta)b) - b) + \beta \mathbb{E}_{\mathbf{s}'\mathbf{i}\mathbf{s}} \left[v^{0}(b';\mathbf{s}') \right] \right\}$$
(12)

Under default, the value function is given by:

$$v^{d}(\mathbf{s}) = u(y - \phi(y)) + \beta \mathbb{E}_{\mathbf{s}'\mathbf{s}} \Big[\mu v^{0}(\mathbf{0}; \mathbf{s}') + (1 - \mu) v^{d}(\mathbf{s}') \Big]$$
(13)

where, in order to keep the environment as simple as possible, we assume that when the government gains re-access to financial markets it does so with no debt obligations (i.e. it gets a "fresh start").¹⁴ Next, we define the recursive equilibrium of this economy.

Definition 1. The recursive equilibrium for this economy is characterized by

- 1. a set of value functions v^0 , v^c , and v^d ,
- 2. a default policy rule d and a borrowing policy rule b',

3. a bond price function q,

such that:

- (a) given the default and borrowing policy functions, v^0 , v^c , and v^d satisfy Eqs. (11)–(13) when the government can trade bonds at q;
- (b) given the default and borrowing policy functions, the bond price function q is given by Eq. (10);
- (c) the default and borrowing policy functions d and b' solve the dynamic programming problem defined by Eqs. (11)–(13) when the government can trade bonds at q.

4. Numerical solution

We solve the model numerically using value function iteration on a discrete state space.¹⁵ We focus on Markov-perfect equilibria. We solve for the equilibrium of the finite-horizon version of our economy, and we increase the number of periods of the finite-horizon economy until value functions and bond prices for the first and second periods of this economy are sufficiently close. We then use the first-period equilibrium objects as the infinite-horizon economy equilibrium objects.

The functional form for the period utility is:

$$u(c) = \frac{c^{1-\gamma}}{1-\gamma} \tag{14}$$

where γ is the coefficient of relative risk aversion. As in Chatterjee and Eyigungor (2012), we assume a quadratic loss function for income during a default episode:

$$\phi(y) = \max\left\{0, d_0 y + d_1 y^2\right\}$$
(15)

As explained by Chatterjee and Eyigungor (2012), this functional form for the income loss $\phi(y)$ is flexible enough to accommodate many cases. If $d_0 > 0$ and $d_1 = 0$, then the cost is proportional to income; if $d_0 = 0$ and $d_1 > 0$, then the cost increases more than proportionately with income; if $d_0 < 0$ and $d_1 > 0$, then the cost is zero in a region ($0 < y < -d_0/d_1$) and then increases faster than income (for $y > -d_0/d_1$). This last case is similar to Arellano (2008)'s cost-of-default function.

4.1. Calibration

We define as "full model" the one in which all the shocks are present. This full model is calibrated to a quarterly frequency using data from a group of 13 emerging economies for the years 1994–2008.¹⁶ These countries and time frame are the union of those used in Foley-Fisher and Guimaraes (2013) and Arora and Cerisola (2001) since we intend to compare the predictions of our model to these empirical studies.

¹⁴ For studies with positive recovery rates and renegotiation between sovereigns and lenders, see for example Yue (2010), D'Erasmo (2011), and Hatchondo et al. (2016).

¹⁵ We use Tauchen (1986)'s method to discretize the income shock and Rouwenhorst's method to discretize the interest rate level shock and the interest rate volatility shock (as suggested by Kopecky and Suen, 2010). The results in Section 5 are obtained using the following grids: 200 points for *b*, 35 points for *y*, 7 points for *r*, and 7 points for *σ*_r. Our results are robust to increasing the grid sizes by 50% in each dimension at a time, and in all dimensions simultaneously (see Johri et al., 2020 Appendix E).

E). ¹⁶ As is common in the sovereign default literature, we focus on time series that exclude default crises. The appendix has details of the country coverage and data definitions: whenever possible, we follow Catao and Mano (2017).

Table 1

Parameters of Full Model Economy.

Household risk aversion	γ	2	Standard value
Household's discount factor	β	0.96	Standard value
Mean int'l risk-free rate	r	0.01	Standard value
Income autocorrelation coefficient	ρ_{v}	0.933	Estimated
Std. dev. of income innovations	σ_{ε}	0.027	Estimated
Probability of re-entry	μ	0.0385	Chatterjee and Eyigungor (2012)
Coupon decay rate	δ	0.0742	Average debt duration
Lenders' risk aversion	κ_{v}	8.75	Calibrated to fit targets
Default cost parameter	d_0	-0.47	Calibrated to fit targets
Default cost parameter	d_1	0.60	Calibrated to fit targets

Table 1 has the parameter values.

We estimate Eq. (1) using quarterly real GDP data. The re-entry probability μ is set to 0.0385 according to Chatterjee and Eyigungor (2012).¹⁷

We assume the representative agent in economy has a coefficient of relative risk aversion γ of 2, the typical value in the literature. The average risk-free rate and the domestic discount factor ($\bar{r} = 0.01$ and $\beta = 0.96$) are standard in quantitative business cycle and sovereign default studies. We set $\delta = 7.42\%$. This value implies a risk-free duration for the sovereign debt of 3 years, which is close to the average duration found in previous literature.¹⁸

We are left with three parameters to assign values to: the parameter controlling the risk premium, κ_y , and the coefficients of the default cost function, d_0 and d_1 . We calibrate these three parameters to the median values of the debt-to-income ratio (44%), the sovereign spread (4.1%), and the standard deviation of the spread (1.9%). All the data counterparts are the medians observed in our panel of emerging economies.

Table 2 presents the parameterization of the stochastic processes that govern the behavior of the world interest rate. We estimate Eqs. (8) and (9) using data on the real international risk free rate for the period 1990 - 2017.¹⁹ We obtain this rate by subtracting expected inflation from the quarterly US T-bill rate. Following Neumeyer and Perri (2005) and Fernández-Villaverde et al. (2011), we compute expected inflation as the average of the US CPI inflation in the current quarter and in the 3 preceding quarters. Parameter values in Table 2 correspond to the median of the posterior estimates. These posterior estimates imply annualized average standard deviations for the risk-free interest rate of 74 basis points (with only mean volatility) and 97 basis points with both mean and stochastic volatility.

4.2. Model fit

In order to compute the sovereign spread implicit in a bond price, we first compute the yield r^b an investor would earn if it holds the bond to maturity (forever in the case of our bonds) and no default is ever declared. This yield r^b satisfies

$$q_t = \frac{1}{1+r^b} + \frac{1-\delta}{(1+r^b)^2} + \frac{(1-\delta)^2}{(1+r^b)^3} + \dots$$

We then compute a similar constant yield, r^{f} , for an otherwise identical but default-free bond.²⁰ The annualized sovereign spread is computed as $4(r^{b} - r^{f})$.

Having calibrated the model, we first verify its ability to reproduce basic features of emerging economy business cycles and that the targets used in calibration are closely approximated. Table 3 reports several key moments in the data and in our simulations of the full model.²¹

The moments reported in Table 3 are chosen to illustrate the ability of the full model to replicate distinctive business cycle properties of economies with sovereign risk. This table shows that the full model approximates well the moments used as targets

 $q_t^{DF} = \frac{1}{1+r^f} + \frac{1-\delta}{(1+r^f)^2} + \frac{(1-\delta)^2}{(1+r^f)^3} + \dots$

²¹ As in previous studies, we report results for pre-default simulation samples. We simulate the model for 500 samples of 1500 periods each. We then discard the initial 1000 periods of each sample as a burn-in and from the remaining data we extract 500 samples of 26 consecutive years before a default. 26 years (or 104 quarters), is the length of the time series for the US T-bill rate used to estimate the process of the world interest rate.

 $^{^{17}}$ This value for μ implies an average financial exclusion of 6.5 years. Gelos et al. (2011) report an average exclusion of 4.7 years for emerging economies. Uribe and Schmitt-Grohé (2017) find an average exclusion of 8 years.

¹⁸ We use the risk-free Macaulay definition of duration that, with the coupon structure in this paper, is given by $D = (1 + \overline{r})/(\delta + \overline{r})$. Focusing on Mexico (an important emerging economy which is in our dataset), Bianchi and Sosa-Padilla (2020) also target a debt duration of 3 years. Using a sample of 27 emerging economies, Cruces et al. (2002) find an average duration of 4.77 years, with a standard deviation of 1.52 years.

¹⁹ We use the stochvol R package, which implements an efficient algorithm for Bayesian estimation of stochastic volatility models via MCMC methods. See Kastner (2016) for more details on the estimation procedure.

²⁰ The price of a default-free bond (that is otherwise identical to the bond issued by the small open economy) is given by the following functional equation: $q^{DF}(\mathbf{s}) = \mathbb{E}_{\mathbf{s}'|\mathbf{s}} \{m(\mathbf{s}', \mathbf{s})[1 + (1 - \delta)q^{DF}(\mathbf{s}')]\}.$

Therefore, the default-free yield r^{f} , is the constant yield-to-maturity that satisfies:

Table 2

Estimates of the Wo	rld Interest Rate Process.
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Autocorrelation risk-free rate	$ ho_r$	0.908
Mean volatility of int'l risk-free rate	$\bar{\sigma_r}$	-6.2869
Autocorrelation interest vol. shock	$\rho_{\sigma r}$	0.8742
Stochastic vol. of int'l risk-free rate	η_r	0.2632

Table 3

Model fit - targeted and non-targeted moments.

	Data	Full Model
Debt/y (in %)	44	44
Spread (in %)	4.1	4.1
SD (Spread) (in %)	1.9	2.1
sd(c)/sd(y)	1.1	1.6
corr(c,y)	0.8	1.0
corr(Spread,y)	-0.5	-0.8

Note: the standard deviation of a variable x is denoted by sd(x) and the correlation between two variables x and z is denoted by corr(x,z). We detrend the log of income (y) and consumption (c) using the HP filter, with a smoothing parameter of 1600. We report deviations from trend.

(the debt-to-income ratio, and the level and volatility of the sovereign spread) and it is broadly consistent with non-targeted moments in the data: consumption is procyclical and more volatile than income, and the sovereign spread is also countercyclical.

5. Results

In this section, we discuss the implications of introducing time variation in both the level and the volatility of the world interest rate. We begin by showing the response of spreads to a rise in the world interest rate which is substantial on average and highly state-contingent, depending on income, debt levels, and the volatility state. Next, we discuss how borrowing decisions are impacted by the level and volatility of world interest rates. We proceed to show that variability in the world interest rates is a source of international co-movement in borrowing costs. We close this section by comparing the full model to one where the world interest rate is constant, emphasizing the welfare losses associated with interest rate uncertainty.

5.1. Main result: the effect of changes in the risk-free rate on spreads

Here we present and discuss the main results of the paper. In particular, we study the response of the sovereign spreads to changes in the world interest rate and highlight how this response is highly state contingent (that is to say, it depends on the actual levels of income, debt and volatility at which these rate movements occur).²²

Reading Eqs. (5) and (6) we first note that if lenders face a higher *r*, then the lenders' stochastic discount factor $(m_{t,t+1})$ and the bond price (q) will mechanically fall (implying higher sovereign yields). On top of this purely mechanical pass-through of higher borrowing costs (from the lenders to the borrower), there will be additional effects due to the equilibrium response of the sovereign.

The higher yields change the default incentives (and therefore sovereign spreads) of the sovereign through two main forces. First, higher borrowing costs imply that more consumption must be sacrificed in order to roll-over existing debt, ceteris paribus, which lowers the desire to repay. Second, since *r* follows a persistent process, higher borrowing costs today are likely to remain in place in the near future. This makes the threat of financial exclusion less severe, as the periods in which the sovereign would be unable to borrow would likely be periods of high borrowing costs. Both forces go in the same direction, increasing incentives to default and (ceteris paribus) increasing the spreads.

Fig. 1 illustrates the dynamics just described above. It shows how the sovereign spread reacts to changes in the world interest rate as a function of the income level. The first thing to notice is the asymmetric response of the spread along the income dimension: for low income levels the increase in spreads can be very large (with $\frac{\Delta \text{Spread}}{\Delta rl}$ being larger than 3 if income is 10% below mean) while it is negligible when income is above mean.²³ The second thing to notice is how the response of spreads depends on the volatility of the world interest rate. Panel (a) of Fig. 1 keeps debt at the mean level observed in the simulations and varies σ_r . The solid blue line refers to the high volatility state while the dashed red line to the low volatility state. We find that, other

²² Henceforth we refer to 'low' and 'high' values of *r* and σ_r to illustrate the state-contingent nature of the effects. Low and high values of *r* and σ_r refer to values that are 4 standard deviations below and above mean.

²³ Notice that the effect can even be slightly negative for high income levels. The rationale is straightforward. The spread is computed as the (annualized) difference between the implied yield of a sovereign bond and the yield on an otherwise identical but default-free bond. The sovereign yield is *always* increasing in *r* (making the borrowing costs higher) but so is the default-free yield. At high income levels the latter increases slightly more, which accounts for the small negative effect on spreads.

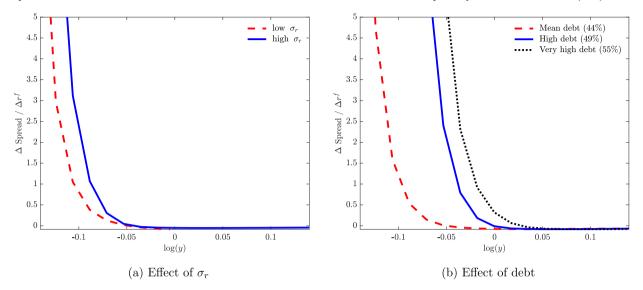


Fig. 1. Spread slopes (Δ Spread $/\Delta r^{f}$). The left panel keeps b' at its mean and the right panel keeps σ_r at its mean. This figure is constructed for a 100 bps increase in the world interest rate. In both panels we allow future debt levels to be chosen optimally.

things equal, the impact of changes in the world interest rate on the sovereign spread is larger in high volatility states. Again, this difference is materially important at low income levels and essentially zero above mean income. The third result to highlight is how the effect depends on the debt chosen by the government. Panel (b) of Fig. 1 makes it clear that the impact of increases in the world interest rate on spreads are amplified by higher debt levels. For example, if the economy is in a moderate recession (with quarterly income being 5% below mean) the spread slope is close to zero under the mean debt level but close to 2 if the debt level is only 5% higher (at 49% of GDP instead of 44%).

Overall, how big is the effect in the model simulations? We focus on reasonable changes in the default-free yield (5–25 bps), keeping *b*' constant (while allowing future levels of debt to vary according to the optimal policy rules), and letting income vary up to 2 standard deviations around its mean value. Within these empirically relevant boundaries, we compute the *spread slope* $\left(=\frac{\Delta S pread}{\Delta r}\right)$ and find that when evaluated at mean volatility it is 1.4. The impact of volatility on the spread slope is quite substantial – it is 0.8 at the low volatility state and 6.4 at the high volatility state. This highlights the highly state contingent interaction of the level and volatility of the risk-free rate. We conclude that the model is able to produce effects of shocks to the world interest rate on sovereign spreads that are in line with the empirical evidence (a *spread slope* of roughly 1), as presented in Foley-Fisher and Guimaraes (2013) and Arora and Cerisola (2001).²⁴

5.2. Effect on borrowing decisions

Fig. 2 shows the effect of different levels of the world interest rate on borrowing decisions as reflected in the debt issuance, for two different volatility levels.²⁵ It is clear from this figure that the small open economy borrows more when lenders face a low world interest rate compared to when lenders face a high interest rate. The issuance function for the low *r* level lies consistently above the one for high *r* level. This pattern can be seen at both low and high volatility levels in panels (a) and (b) respectively, with an increase in volatility magnifying the effect.

These issuance policy function responses to interest rate changes are reflected in the simulations. In order to quantify these responses we follow the previous section and define the *issuance slope* as $\frac{\Delta t}{\Delta r^{f}}$. Holding the volatility state at its mean, we find an issuance slope of -2.7, on average. The impact of volatility on the issuance slope is also substantial: it is -0.5 at the low volatility state and -5.6 at the high volatility state. This, once again, highlights the impact of the volatility state on model responses.

5.3. International co-movement in sovereign yields

Time variation in the world interest rate not only increases the level and volatility of a country's borrowing costs (its sovereign yield) but it can potentially create co-movement between the yields of various countries. To illustrate and quantify this natural implication of our model we perform the following exercise: (i) we draw multiple random (and independent) samples for the

²⁴ The way we compute the spread slope, keeping *b'* constant, is in the spirit of a common empirical strategy in which the spread response is calculated over a window that is short enough that debt is assumed not to immediately react to the interest rate shock. In both the model and empirical exercises, rational agents will naturally price the sovereign bonds anticipating future movements in debt.

²⁵ The focus on the response of debt issuance in our paper is equivalent to the focus on debt changes in the literature with one-period debt. An equivalent analysis of debt-responses can be found in the Appendix.

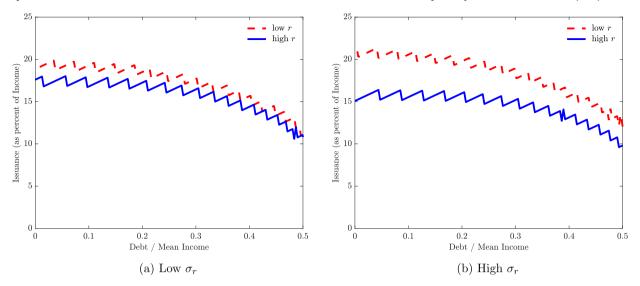


Fig. 2. Effect of interest rate on debt issuance. The left panel is for a low level of σ_r and the right panel is for a high level of σ_r . The solid blue line is for high *r* while the red dashed line is for low *r*. Both panels are for the mean income level. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

income process, (ii) we select the two samples that have the most similar pairwise income correlation to the data (0.50 in the simulations and 0.57 in the data), (iii) we feed these sequences of shocks into our full model along with a common (and independent) sequence of shocks to the world interest rate, (iv) we correlate the sovereign yields between these two samples (which may be thought of as symbolizing two countries), and (v) finally, we condition the correlation calculation on debt lying 2 percentage points above and below the mean. We find this correlation to be large (0.40) and significant.²⁶

We repeat the same process for our 'basic model' where the world interest rate is constant (i.e., we set $u_r = u_{or} = 0$ while leaving all other parameters unchanged at their values in the full model) and find a correlation coefficient that is much lower (0.17) and insignificant.²⁷ The higher correlation in the full model suggests that global interest rate shocks may play a nontrivial role in generating the observed international co-movement in yields found in our data (a mean correlation between sovereign yields of 0.53).²⁸

5.4. Welfare effects

Having shown that variation in the world interest rate can have state-contingent impacts on the borrowing costs of our "full model" economy, we now wish to quantify the welfare consequences of this variation. To do this we ask: what are the welfare gains of living in the full model as compared to the basic model economy? Fig. 3 plots these gains as a function of the income level. The gains are expressed as the constant proportional change in consumption that would leave a consumer indifferent between living in the full model or the basic model where r is constant. We present results for two scenarios. In scenario 1, initial debt is zero while in scenario 2, the economy starts at the mean level of debt.

When initial debt is zero (solid green line), the average (across income levels) welfare gain is 0.01% of permanent consumption. Note that in this case the welfare gains are decreasing in the income level. For the case with positive initial debt (dashed black line), there are some interesting non-monotonicities at work. At low income levels, the welfare gains are particularly low since default is more likely and the value of defaulting ($v^d(\mathbf{s})$) under no interest rate uncertainty is not dramatically higher than with uncertainty. However, for intermediate levels of income, the welfare gains are higher because it is precisely in these states where the basic model implies that the government is able to repay existing debt and also borrow at cheaper rates than in the full model. The average welfare gain of eliminating all uncertainty about the world interest rate in this case (with initial debt equal to the mean level observed in the simulations) is equal to a 0.02% constant increase in consumption.

6. Conclusions

We have introduced time-varying volatility in the world interest rate in a standard sovereign default model with long term debt. The process for the world interest rate includes both mean volatility (i.e., shocks to the level of the interest rate) and

²⁶ Not conditioning on debt levels produces a very similar result (a significant correlation of 0.42).

 $rac{27}{r}$ There are two possible conceptual ways to decompose the full model – the basic model with no movement in *r* and the 'intermediate model' which incorporates shocks to the level of *r* but not to its volatility. A discussion of these models and the corresponding moments can be found in appendix D of Johri et al. (2020).

²⁸ For this exercise we use quarterly sovereign yields data from Longstaff et al. (2011). The appendix has the details of the data as well as a complete spread correlation matrix.

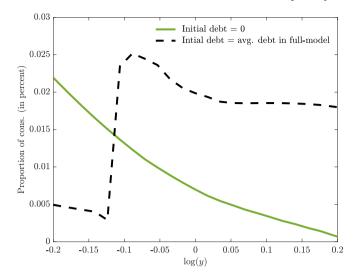


Fig. 3. Welfare gains of moving from the full to the basic economy. The initial debt levels are zero in the solid green line, and the mean in the simulations (44%) in the dashed black line. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

stochastic volatility (i.e., shocks to the volatility of the interest rate). Time variation in the world interest rate interacts with default incentives and its effect on borrowing and sovereign spreads is state contingent. We find that the change in spread is on average 1.4 times the increase in the world interest rate when volatility is at its mean. This 'slope' increases to 6.4 when volatility state is high and falls to 0.8 when volatility is low. Not surprisingly, higher debt makes the spread response to the world interest rate stronger.

In our model, the common process for the world interest rate acts as a global factor with the potential to generate international co-movement in sovereign yields. We quantify this by comparing simulations from the basic and full models: independent economies featuring uncorrelated borrowing costs under the basic model would produce times series for their sovereign yields that have a positive and significant correlation under the full model (i.e., with a common stochastic process for the world interest rate).

We find positive welfare gains from eliminating uncertainty about the world interest rate and these potentially justify the concerns expressed by policy makers in the face of an increase in uncertainty about the path of the world interest rate.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Appendix A. Supplementary data

Supplementary data to this article can be found online at https://doi.org/10.1016/j.jinteco.2022.103681.

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